Complex Zeros

Difference & Sum

of Squares

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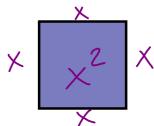
Notes

$$\frac{4-2i}{4+6i}$$
 $\frac{4-6i}{4-6i}$
 $\frac{16-24i-8i+12i^2}{16-24i+24i}$
 $\frac{32i}{52}$
 $\frac{4-32i}{52}$
 $\frac{1}{52}$
 $\frac{8i}{13}$
 $\frac{1}{13}$

Objective: To be able to find complex roots of a polynomial and write a polynomial given its real and complex roots.

Life Lesson/Math Skill: To be able to solve and find all roots of any polynomial. Sometimes you do things because you can.

What makes a perfect square?



What do you think a difference of squares is?

Difference of Squares

$$ax^2 - c = (\sqrt{ax} - \sqrt{c})(\sqrt{ax} + \sqrt{c})$$

Notice: 2 terms (binomial), and a and c are perfect squares AND c is subtracted

Step 1: Factor out GCF first.

Step 2: Find the square root of the first and last numbers a and c

Step 3. Write the new factors where one is added and the other is subtracted (this would cancel the middle term if you were to check your work and distribute)

ex.
$$4x^2 - 25$$

 $74x^2$ 725
 $(2x+5)(2x-5)$

ex.
$$9x^2 - 36$$

 $9(x^2 - 4)$
 $9(x + 2)(x - 2)$

ex.
$$1/64p^2 - 169$$

$$\frac{\sqrt{1}}{\sqrt{64}}\sqrt{p^2} \sqrt{169}$$

$$(\frac{1}{8}p + 13)(\frac{1}{8}p - 15)$$

ex.
$$-18p^{2} + 48$$
 $-18p^{2}$
 $-18p^{2}$

$$2(216+3p)(216-3p)$$

$$2\sqrt{6} + 3\rho = 0
3\rho = -2\sqrt{6}
\rho = -2\sqrt{6}
+ \sqrt{24} = \rho^{2}
+ \sqrt{24} = \rho^{2}
- 3$$

Irreducible Factors

Factors that cannot be factored into linear factors without using imaginary numbers

ex.
$$x^4 + 2x^2 - 8 - 0$$
 $(x^2 + 4)(x^2 - 2) = 0$
 $(x^2 + 4)(x^2 - 2) = 0$
 $(x - 2i)(x + 2i)(x + \sqrt{2})(x - \sqrt{2}) = 0$
 $(x - 2i)(x + 2i)(x + \sqrt{2})(x - \sqrt{2}) = 0$
 $(x - 2i)(x + 2i)(x$

Sum of Squares

 $ax^2 + c = (\sqrt{ax} \cdot j \cdot \sqrt{c})(\sqrt{ax} \cdot \beta i \cdot \sqrt{c})$

Notice: 2 terms (binomial), and a and c are perfect squares AND c is added

Step 1: Factor out GCF first.

Step 2: Find the square root of the first and last numbers a and c

Step 3. Write the new factors as complex conjugates with *i* (this would cancel the middle term if you were to check your work and distribute)

ex.
$$16x^{2} + 49$$
 ex. $81x^{6} + 121$

$$(4x+7)(4x-7)$$

$$(9x^{3}+||||)(9x^{3}-||||)$$
ex. $p^{2}+1/144$ ex. $-18p^{2}-200$

$$(p-12)(p+12)(p+12)(p+12)(p+100)$$

$$(p^{2}+12)(p+12)(p+12)(p+100)$$

$$(p^{2}+144)(p+12)(p+12)(p+100)$$

$$(p^{2}+144)(p+12)(p+12)(p+100)$$

$$(p^{2}+144)(p+12)(p+12)(p+100)$$

$$(p^{2}+144)(p+12)(p+12)(p+1000)(p+100)(p+1000)(p+1000)(p+1000)(p+1000)(p+1000)(p+1000)(p+1000)(p+1000)(p+1000)(p+1$$

Remember: It is the simple things in life....

The Zero Product Property

Anything times 0 equals 0





if ab = 0 then either b was 0 or a was 0

There it is! Use your new skills to solve the equation.

$$3b^{3} = 27b = 0$$

$$3b(b^{2} - 9) = 0$$

$$3b(b^{2} - 9) = 0$$

$$3b(b^{2} - 4)(d^{2} + 4) = 0$$

$$3b(b + 3)(b - 3) = 0$$

$$3b = 0$$

$$3b = 0$$

$$b = 0$$

Homework: <u>Factor</u> each by using the Difference or Sum of Squares <u>then</u> Solve using 0 product property.

1.
$$81x^2 - 49 = 0$$

2.
$$36n^2 = -1$$

3.
$$49 - 25x^2 = 0$$

4.
$$\frac{1}{4}x^2 + 104 = 4$$

5.
$$\frac{81}{256} = 16$$
m⁴

6.
$$48n^7 = 147n$$

Homework: Factor and Solve each Difference or Sum of Squares.

1.
$$81x^{2} - 49 = 0$$

 $(9 \times -7)(9 \times +7) = 0$
 $9x - 7 = 0$ $9x + 7 = 0$
 $1 \times = \frac{7}{9}$ $1 \times = -\frac{7}{9}$

3.
$$49 - 25x^2 = 0$$

 $(7-5x)(7+5x)=0$
 $7-5x=0$ $7+5x=0$
 $x=\frac{7}{5}$ $x=-\frac{7}{5}$

5.
$$\frac{81}{256} = 16m^4$$
 $16m^4 - \frac{81}{256} = 0$
 $(4m^2 - \frac{9}{16})(4m^2 + \frac{9}{16}) = 0$
 $(4m^2 - \frac{9}{16})(4m^2 + \frac{9}{16}) = 0$
 $(2m - \frac{3}{4})(2m + \frac{3}{4})(2m + \frac{3}{4}i)(2m - \frac{3}{4}i) = 0$
 $(2m - \frac{3}{4})(2m + \frac{3}{4}i)(2m + \frac{3}{4}i)(2m - \frac{3}{4}i) = 0$
 $(2m - \frac{3}{4})(2m + \frac{3}{4}i)(2m + \frac{3}{4}i)(2m - \frac{3}{4}i) = 0$
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 $(2m - \frac{3}{4})(2m + \frac{3}{4}i)(2m + \frac{3}{4}i)(2m + \frac{3}{4}i)(2m + \frac{3}{4}i) = 0$
 $(2m - \frac{3}{4})(2m + \frac{3}{4}i)(2m +$

2.
$$36n^2 = -1$$

 $36n^2 + 1 = 0$
 $(6n+i)(6n-i) = 0$
 $6n+i=0$ $6n-i=0$
 $n=-\frac{i}{6}$ $n=\frac{i}{6}$

$$49 - 25x^{2} = 0$$

$$(7-5x)(7+5x)=0$$

$$7-5x=0$$

$$(-5x)(7+5x)=0$$

$$(-5x)(7+5x)=0$$