

Algebra 2 SAT Prep Wkst 1

1. $\frac{5x}{6y} \cdot \frac{3}{10y}$

Which expression is equivalent to the above product for all $y \neq 0$?

- A $x/2$
- B $(25x)/9$
- C $x/(2y^2)$
- D $x/(4y^2)$

$\frac{5x}{6y} \cdot \frac{3}{10y}$ When multiplying fractions by $\frac{3}{10y}$ multiply straight across
 $\frac{15x}{60y^2} = \frac{1x}{4y^2}$

2. What is the sum of $3b(b-4)$ and $6(b-8)$?

- A $3b(1-2b-16)$
- B $3b(b-2-16)$
- C $3(b^2-2b-16)$
- D $3(b^2-2-16b)$

$3b(b-4) + 6(b-8)$ distribute
 $3b^2 - 12b + 6b - 48$ add + combine like terms
 $3b^2 - 6b - 48$ Factor by dividing out common factor and put outside parentheses
 $3(b^2 - 2b - 16)$ like undoing distribution

3. Which of the following expressions is equivalent to $(3c^3 - 4c^2 + c) - (5c^2 - 6c^3 - 9c)$?

- A $7c^3 + 9c^2 - 3c$
- B $7c^3 + c^2 - 3c$
- C $-7c^3 + c^2 + 9c$
- D $-7c^3 - 9c^2 + 9c$

$3c^3 - 4c^2 + c - 5c^2 - 6c^3 - 9c$ distribute subtraction
 $-7c^3 - 9c^2 + 9c$ watch for sign changes

4. $P(x) = 2x^3 - 18x$ Factor out GCF

$2x(x^2 - 9) \rightarrow 2x(x-3)(x+3)$ Factor difference of Squares
 $2x=0 \quad x-3=0 \quad x+3=0$

Given the polynomial function defined above, what are its zeros?

Factor and set each factor = 0

- A -9, -6, 2, 3
- B -9, 0, 2
- C -3, 0, 3

$x=0 \quad x=3 \quad \text{and} \quad x=-3$

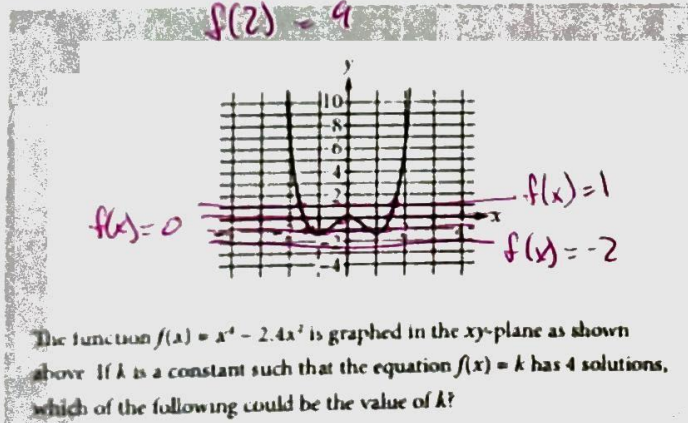
25. If $g(x) = 2x + 1$ and $f(x) = g(x) + 4$, what is $f(2)$?

- A 5
- B 6
- C 9
- D 11

$f(2) = g(2) + 4$
 $f(2) = [2(2) + 1] + 4$
 $= [4 + 1] + 4$
 $f(2) = 5 + 4$
 $f(2) = 9$

means $x=2$ plug 2 in for x so first plug 2 in for x for $g(x)$ then plug what you got in for $g(x)$

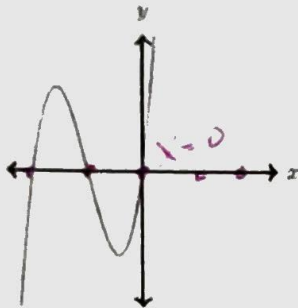
26.



$f(x) = k$ is a horizontal line must cross function 4 times to have 4 solutions

- A -2 doesn't cross any times 0 solutions
- B -1 Crosses 4 times
- C 0 crosses 3 times there is a bounce at $(0,0) \quad x=0$
- D 1 Crosses 2 times so 2 solutions

5.



Which of the following functions could represent the graph in the x, y -plane, where $y=P(x)$?

3 solutions
so must be x^3
not x^2
Factor out x
and factor quadratic

$$\begin{aligned} & x^3 + 6x^2 + 8x \\ & x(x^2 + 6x + 8) \\ & x(x+4)(x+2) \end{aligned} \left\{ \begin{aligned} & x^3 - 6x^2 + 8x \\ & x(x^2 - 6x + 8) \\ & x(x-4)(x-2) \end{aligned} \right.$$

$x=0$ $x+4=0$ $x+2=0$ $x=0$ $x-4=0$
 $x=-4$ $x=-2$ $x=4$ $x=2$

- A $P(x) = x^2 + 6x + 8$ would look like \cup or \cap
- C $P(x) = x^2 - 6x + 8$
- D $P(x) = x^3 + 6x^2 + 8x$
- $P(x) = x^3 - 6x^2 + 8x$

Graph on graphing calculator

6. A polynomial has zeros at -9, 2, and 0. Which of the following could be the polynomial?

- A $x^2 - 7x - 18$ can't be there are 3 zeros & degree should be 3
- C $x^3 + 8x^2 - 11x - 18$
- D $x^3 + 6x^2 - 25x + 18$ $x=0$ is a zero so all terms will have x

$x = -9$ $x = 2$ $x = 0$
 $+9$ $+9$ -2 -2
 $x+9=0$ $x-2=0$ $x=0$
 $x(x+9)(x-2)$
 $x(x^2 + 7x - 18)$
 $x^3 + 7x^2 - 18x$

7. Let $g(x) = 8x - 5$. Which of the following is equivalent to $g(g(x))$?
- A $64x - 10$
- C $64x^2 + 25$
- $64x - 45$
- D $64x^2 - 80x + 25$

$g(g(x))$
is a composition
it means
put the whole
function $g(x)$
in for the x
of the outer
function $g(x)$
the function
completely
replaces x

8. $C = 1.2272M + 3.0556F$

An English teacher uses the equation above to give the composite score, C , on the final exam, given M correct multiple choice answers and F points on the free response questions. Which of the following equations correctly gives the number of correct multiple choice answers in terms of the composite score and the number of points on the free response questions? Solve for M

- $M = (C - 3.0556F) / 1.2272$
- C $M = (3.0556F - C) / 1.2272$
- B $M = (C / 1.2272) - 3.0556F$
- D $M = (3.0556F / 1.2272) - C$

$$\begin{aligned} C &= 1.2272M + 3.0556F \\ C - 3.0556F &= 1.2272M \\ \frac{C - 3.0556F}{1.2272} &= \frac{1.2272M}{1.2272} \\ &= M \end{aligned}$$

$(a+b+c)(a+b+c)$

9. $(a+b+c)^2$

Which of the following is equivalent to the above expression?

A $a^2+b^2+c^2+2(ab+bc+ca)$

B $a^2+b^2+c^2$

C $a^2+2abc+c^2$

D $a^2+2ab+b^2+2bc+c^2$

$a(a+b+c) + b(a+b+c) + c(a+b+c)$
 $a^2 + ab + ac + ba + b^2 + bc + ca + cb + c^2$
 $a^2 + 2ab + 2bc + 2ca + b^2 + c^2$
 all have 2 so factor it out
 $a^2 + b^2 + c^2 + 2(ab+bc+ca)$

10. Which of the following represents all solutions (x,y) to the system of equations shown below?

$y = x - 2$
 $y = x^2 - x - 5$

you could graph both functions and see where they cross or substitute and solve for x

$x - 2 = x^2 - x - 5$
 $-x + 2 \quad -x + 2$
 $0 = x^2 - 2x - 3$
 $0 = (x-3)(x+1)$

A (3, -1)

B (-3, 1)

C (3, -5) and (1, -1)

D (3, 1) and (-1, -3)

$x+3=0 \quad x+1=0$
 $x=-3 \quad x=-1$

11. $-7x^2 = (y+5)(y-5)$

$5y = 15x \rightarrow y = \frac{15x}{5} = 3x$

$\rightarrow -7x^2 = (3x+5)(3x-5)$
 $-7x^2 = 9x^2 - 15x + 15x - 25$
 $-7x^2 = 9x^2 - 25$

If (a,b) is a solution to the system of equations shown above and $a > 0$, what is the value of a?

A 1/2

B 1

C 5/4

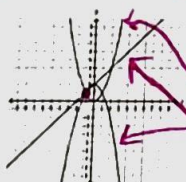
D 3

alphabetical order
 $a = x \quad b = y$

$0 = 10x^2 - 25$
 $0 = (4x-5)(4x+5)$
 $4x-5=0 \quad 4x+5=0$
 $x = 5/4 \quad x = -5/4$

values for x
 $x = 3 \quad x = -1$
 $y = (3) - 2 = 1$
 $y = (-1) - 2 = -3$

12.



The system of equations represented by the graph in the xy-plane at left is $y = x^2$, $y = x + 2$, and $y = -x + 3$. Which of the following lists all solutions to the system of equations?

A (-1, 1)

B (0, 2)

C (0, 2) and (2, 4)

D (-1, 1), (1, 1), (0, 2) and (2, 4)

points that work for all 3 at the same time

13. $(2x-3)(x+4) = 0$

Let $x = a$ and $x = b$ be the solutions to the equation above. What is the value of $a + b$?

A -5/2

B -1/2

C 5/2

D 9.5

Separate set = 0 and solve
 $2x-3=0 \quad x+4=0$
 $2x=3 \quad -4 \quad -4$
 $x=3/2 \quad x=-4$

you need to know what the two solutions are and then add them together

$\frac{3}{2} + \frac{-4}{1} = \frac{3}{2} - \frac{8}{2} = \frac{-5}{2}$

To add or subtract fractions get common denominator multiply top + bottom by same # so denominators match

14. $P(x) = -0.31(x - 260)^2 + 9500$
 A shoe manufacturer determines that its monthly revenue $P(x)$ in dollars is a function of the number of shoes x that it sells each month. What is the maximum dollar amount of the company's monthly revenue in dollars?

- A 260
- C 7000

Vertex Form
 (260) (1500)
 shoe sale revenue
B 9500
B 2945

15. A factory designs cylindrical cans 10 cm in height to hold exactly 500 cm³ of a liquid. Which of the following best approximates the radius of these cans?

- A 4 cm
- C 12.5 cm

Find radius r
 $V = BH$
 $V = \pi r^2 \cdot H$
 $500 = \pi r^2 \cdot 10$
 $\frac{500}{10} = \frac{\pi r^2 \cdot 10}{10}$
 $50 = \pi r^2$
 $r = \sqrt{\frac{50}{\pi}}$

16. Leo throws a stone vertically upward from a bridge. The height, in meters, of the stone t seconds after it is thrown is modeled by the quadratic function $h(t) = -4.9t^2 - 9.8t + 39.2$. After how many seconds does the stone hit the water?

- A 1 second
- C 4 seconds

use quadratic formula
 $h(t) = 0$ solve for t
 graph on calculator
B 2 seconds
 -1 seconds doesn't make sense

17. The following function gives the amount of money owed on a short term loan after t years: $A(t) = 100 \cdot (1.25)^t$. Which numerical expression best approximates the annual interest rate, excluding (1 year = 52 weeks)?

- A $1 - (0.25)^{26}$
- C $(26)(1.25)$

$100(1.25)^{52/2}$
 $100(1.25)^{26}$
B $1.25^{26} - 1$
 closest

18. If $b^3 \cdot (b^4)^2 = b^x$, what is the value of x ?

- A 9
- C 18

$b^3 \cdot b^8 = b^x$
 $b^{3+8} = b^x$
 $3+8 = x$
 $11 = x$
B 11
D 19

19. What is the sum of the solutions to the equation below?

add both solutions
 $(y-3) = (\sqrt{7y-31})^2$ square both sides to undo $\sqrt{\quad}$
 $(y-3)(y-3) = 7y-31$

- A -13
- C 3

$y^2 - 6y + 9 = 7y - 31$
 $-7y + 31 -7y + 31$
 $y^2 - 13y + 40 = 0$
 $(y-8)(y-5) = 0$
 $y-8=0 \quad y-5=0$
 $y=8 \quad y=5$
 $8+5 = 13$
B -3
B 13

20. What is the sum of the solutions to the above equation?

$3p+13 = (p+3)(p+3)$
 $3p+13 = p^2 + 6p + 9$
 $-3p - 13 = p^2 - 4p - 4$
 $0 = p^2 + 3p - 4$
 $(p+4)(p-1) = 0$
 $p+4=0 \quad p-1=0$
 $p=-4 \quad p=1$
 $-4+1 = -3$
A -3
B 0
D 2

21. For what values of x is $f(x) = 2x^2 + 2$ equal to $g(x) = x^2 + x + 2$?

- A -1 and 0
- C 1 and 2

$2x^2 + 2 = x^2 + x + 2$
 $-2x - 2 = -2x - 2$
 $0 = x^2 - x$
 $0 = x(x-1)$
 $x=0 \quad x-1=0 \quad x=1$
B 0 and 1
D 2 and 3

22. If $x > 0$ and $2x^2 + 3x - 2 = 0$, what is the value of x ?

- A -2
- C 1/2

$2x^2 + 4x - 1x - 2 = 0$
 $(x+2)(2x-1) = 0$
 $x+2=0 \quad 2x-1=0$
 $x=-2 \quad x=1/2$
 x is positive
B 0
D 1

23. What is the sum of the solutions of $(2x-1)^2 = (x+2)^2$?

- A -3
- C 8/3

$2x-1 = x+2$ and $2x-1 = -(x+2)$
 $-x+1 = -x+2$
 $x=3$
 $x+1 = x+1$
 $3x = -1$
 $x = -1/3$
 $3 + (-1/3) = 8/3$
B 0
D 10/3

24. A researcher estimates that the population of a city is declining at 0.6%. The current population of the city is 80,000, which of the following models the population of the city t years from now?

- A $80,000(1 - 0.006)^t$
- C $80,000 - 1.006^t$

$A = P(1+r)^t$
 $A = 80000(1 - 0.006)^t$
B $80,000(1 - 0.006)^t$
D $80,000(0.006^t)$

rate 0.6
 $r = 0.006$
 decline means subtract