## Lessons 1.1-1.3 Worksheet

 Nome: Key Date: $\qquad$Directions: the first two of the equations in each line are partially worked out, you are to fill in the blanks and/or work needed in each step, and apply what you have learned and is done to the last problem in that line.

Two Step Equations

1. $-7 x+24=-11$
$(-24)-24$ $\frac{->x}{-7}=\frac{35}{-7}$
$x=-5$

$x=-6$
2. $7-3 x=-8$


$$
\frac{-3 x}{-3}=\frac{-15}{-3}
$$

$$
x=5
$$

Combining Like Terms First, then solve the two step equation

1. $6 x+4 x-15=25$

$$
\begin{aligned}
& 10 x\binom{-15}{+15}=25 \\
&+15 \\
& \frac{10 x}{10}=-\frac{40}{10}
\end{aligned}
$$

$$
x=-4
$$

2. $-15=3-6 x+15 x$
$-15=3+9 x$
$-3-(-3$
$-\frac{18}{9}=\frac{9 x}{9}$
$-2=x$
3. $23=4 x-7-6 x$

$\frac{30}{-2}=\frac{-2 x}{-2}$
$-15=x$

Combine like terms first, then Move Variable so it is only on one side, last solve the two step equation

1. $\left.\begin{array}{c}7 x-2 x-12=7 x+10 \\ 5 x-12=7 x+10 \\ -5 x) \\ -5 x \\ -12=2 x+10 \\ -10\end{array}\right)$
2. $\begin{aligned} 21-3 x & =-4 x+9-5 x \\ 21-3 x & =-9 x-9 \\ +9 x & +9 x+\end{aligned}$
$\begin{aligned} &\binom{21}{-21} \\ &+6 x_{-}=9 \\ &-21 \\ & \frac{6 x}{6}=\frac{-12}{6}\end{aligned}$
$x=-2$
3. $13 x-7 x+33=-5 x+11$

$11 x\binom{+33}{-33}=-11$

$$
\frac{11 x}{11}=\frac{-22}{11}
$$

$$
x=-2
$$

## Lessons 1.3 and 2.1-2.4 Worksheet name: Key Date:___

Distribute First, combine like terms second, then move variable so it is only on one side, last solve the two step equations

1. $2 x+3(x-4)=7(x+4)$ $2 x+3 x-12=7 x+28$
$-5 x-12=7 x+28$
$-5 x-5 x$
$-12=2 x+28$
-28
-40
$\frac{-40}{2}=\frac{2 x}{2}$
$-20=x$
2. $16-2(x-9)=-12(x+3)+3 x$
$16-2 x+18=-12 x-36+3 x$ $34-2 x=(-9 x-36$
$+9 x_{-}(9 x)$
$\binom{34+7 x=}{-34} \begin{array}{r}-36 \\ -34\end{array}$
$\frac{7 x=-70}{7} \frac{--}{7}$
$x=-10$
3. $11 x-5(x+4)=-2(x-5)+5 x$
$11 x-5 x-20=-2 x+10+5 x$
$6 x-20=3 x+10$
$-3 x-3 x$
$3 x-20=10$
$+20+20$
$3 x=30$
3 3
$x=10$

INEQULAITIES. Solve and Graph. DON'T FORGET TO FLIP THE SIGN WHEN $\bullet \div$ BY A ( - )

$$
\begin{aligned}
& \text { 1. } \begin{array}{c}
3 x-4
\end{array} \leq 8 \\
&(+4)+4 \\
& \frac{3 x}{3} \leq \frac{12}{3} \\
& x \leq-4
\end{aligned}
$$

(does not flip-divided by a positive)

2. $4-3 x>10$
$-4-4$
$\frac{-3 x}{-3}>\frac{-6}{-3}$
$x<-2$
3. $-7 x-16 \geq 19$
$+16+16$
$\frac{-7 x}{-7} \geq \frac{35}{-7}$
$x \leq-5$
(does flip-divided by a negative)

4. $20 \leq 6 x+2$
5. $27>7-4 x$

Rewrite: $7-4 x<35$

$$
\begin{array}{ll}
-7 & --7 \\
\frac{-4 x}{-4} & <\frac{28}{-4}
\end{array}
$$

(does not flip-divided by a positive)
Rewrite: $x \geq 3$

(does flip-divided by a negative)

$$
\begin{aligned}
& -\frac{2}{-}-2 \\
& \frac{-18}{6} \leq \frac{6 x}{6} \\
& -3 \leq x
\end{aligned}
$$

$$
x>-7 \quad x<-5
$$


6. $16<-6 x-14$
$+14+14$
$\frac{30}{-6}<\frac{-6 x}{-6}$
$-5>x$

Name:
 Date: $\qquad$ Combining Like Terms First, then solve the two step inequality


Distribute First, combine like terms second, then move variable so it is only on one side, last solve the two step inequality

1. $4 x+2(3 x-5) \leq 7(x+4)-2$

$$
\text { 2. } 22-5(x-6)>-4(x+9)-5 x
$$

$4 x+6 x-10 \leq 7 x+28-2$

$$
22-5 x+30>-4 x-36-5 x
$$



$$
52-5 x)>-9 x-36
$$

$$
\left.\begin{array}{r}
52>-4 x(-36 \\
+36
\end{array}\right)
$$

$$
\frac{88}{-4} \frac{>-4 x}{-4}
$$

$x \leq 18$

$$
-22<x
$$

$$
\text { Rewrite: } x>-22
$$


$\begin{array}{lll}17 & 18 & 19\end{array}$
3. $13 x-5(x+4)>-2(x-5)+8 x$
$13 x-5 x-20>-2 x+10+8 x$

$$
8 x-20>6 x+10 \quad x>15
$$

$$
\begin{aligned}
2 x-20 & >10 \\
& +20
\end{aligned}
$$



$$
\frac{2 x}{2}>\frac{30}{2}
$$



Finding Slope from Points

1. label the first coordinates $x_{1}$ and $y_{1}$

$$
m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}
$$

2. label the second coordinates $x_{2}$ and $y_{2}$
3. Substitute and simplify

$$
\begin{gathered}
(13,-5),(-9,6) \\
x_{1} y_{1} y_{2} \\
m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}}=\frac{6-5}{-9-13} \\
m=\frac{11}{-22}=-\frac{1}{2} \\
m=-\frac{1}{2}=\frac{-1}{2} \\
\begin{array}{l}
(2,-3),(2,8) \\
x_{1} y_{1} x_{2} y_{2} \\
m=\frac{-3-8}{2-2}=\frac{-11}{0}
\end{array}, \$ \text { m }
\end{gathered}
$$

$$
(5,-4),(7,-4)
$$

$$
x_{1} y_{1} \quad x_{2} y_{2}
$$

$$
m=\frac{-4--4}{7-5}=\frac{0}{2}=0
$$

$$
m=-\frac{1}{2}=\frac{-1}{2}=\frac{1}{-2}=-0.5
$$

$$
(-1,-3),(-2,-8)
$$

$$
x_{1} y_{1} \quad x_{2} y_{2}
$$

$$
m=\frac{-3--8}{-1--2}=\frac{5}{1}=5
$$

slope is undefined

$$
m=5=\frac{5}{1}=\frac{-5}{-1}
$$

Examples: Write the slope and $y$-intercept of each line.

1) $y=2 / 3 x-5$
2) $y=-3 / 5 x-3$

$$
b=-5 \quad(0,-5)
$$

$$
b=-3 \quad(0,-3)
$$

$$
m=\frac{-3}{5}=\frac{-3}{5}=\frac{3}{-5}=-0.6
$$

3) $y=4 x+3$
4) $y=7 / 6 x-8$

$$
\begin{aligned}
& b=3 \quad(0,3) \\
& m=4=\frac{4}{1}=\frac{-4}{-1}
\end{aligned}
$$

$$
b=-8 \quad(0,-8)
$$

Graph each equation using slope and y intercept.

3) $y=6 / 5 x$

2) $y=-x+3$

4) $y=x-5$


Graph each equation and label the $y$-int, AOS, and vertex

$$
\begin{array}{ll}
\text { 1) } y=3 x^{2}+6 x+2 & \text { 2) } y=2 x^{2}-8 x-1
\end{array}
$$



$$
\begin{aligned}
f(2) & =2(2)^{2}-8(2)-1 \\
& =8-16-1 \\
& =-8-1 \\
& =-9
\end{aligned}
$$

## Writing Linear Equations Review

Name 12 Date: $\qquad$ Calculate the slope of the line passing through each pair of points using the slope formula. If the slope is undefined, write "undefined."

1. $(-6,7)$ and $(-6,-2)$

2. $(4,1)$ and $(-4,1)$
$m=0$

3. $(-2,1)$ and (3,-2)


Write the slope-intercept form of an equation for the lines graphed below.
4.

5.


6.


7. Write a linear equation in slope-intercepet form to model the situation: An Skyzone charges $\$ 5.95$ per person plus $\$ 2.50$ for each hour for jumping. Let $y$ be the total amount you pay to jump.

$m=2.50$
$y=2.50 x+5.95$
8. Write a linear equation in slope-intercept form to model the situation: You have $\$ 3,000$ in a bank account, and you set up automatic bill pay for your cellphone bill of $\$ 124.98$ per month. Let y be how much is left in the account each month.

$$
y=3000-124.98 x
$$

Writing Linear Equations Review
Name: $\qquad$ Date: $\qquad$
For question 9-13, write the slope-intercept form of the equation for the line given each situation.
9. Passes through $(5,4)$ and $(6,-1)$
$m=\frac{4-1}{5-6}-\frac{5}{-1}=-5$

$$
4=-25+b
$$

$$
+25+25
$$

$$
y=-5 x+29
$$



$$
2.9=b
$$

11. Passes through $(-4,-5)$ and ( $6,-1$ )

$$
\begin{aligned}
& m=\frac{-5-1}{-4-6}=\frac{-4}{-10}=\frac{2}{5} \\
& -5=\frac{2}{5}(-4)+b \\
& \frac{-25}{5}=\frac{-8}{5}+b \quad y=\frac{2}{5} x-3.4 \\
& -\frac{17}{5}=b
\end{aligned}
$$

13. Perpendicular to the graph of $4 x-y=12$ that passes through $(8,2)$

$$
\begin{aligned}
& -4 x \\
& \frac{-4}{-1}=\frac{-4 x+12}{-1} \\
& y=-4 x-12 \quad 2=\frac{1}{4}(8)+b \\
& m=-4=\frac{-4}{1} \quad 2=2+b \\
& m \perp=\frac{1}{4} \quad \begin{array}{l}
\quad-2-2 \\
y=\frac{1}{4} x
\end{array}
\end{aligned}
$$

10. Slope of $\frac{4}{3}$ and passes through $(3,0)$

$$
\begin{aligned}
0 & =\frac{4}{3}(3)+b \\
0 & =4+b \\
-4 & =b
\end{aligned}
$$

12. Parallel to the graph of $9 x+3 y=6$ that passes through $(5,3)$

$$
\begin{array}{ll}
9 x+3 y=6 & y=-3(5)+b \\
-4 x & -4 x \\
\frac{3 y}{3}=-\frac{-4 x+6}{3} & 18=-15+b \\
y=-3 x+2 & y=-3 x+18
\end{array}
$$

$m=-3$
14. Perpendicular to the graph of $y=-\frac{2}{3} x+18$ that passes through $(0,2)$

$$
\begin{array}{ll}
m=-\frac{2}{3} & 2=\frac{3}{2}(0)+b \\
m \perp=\frac{3}{2} & 2=b \\
y=\frac{3}{2} x+2
\end{array}
$$

You will be factoring or solving all the expressions or equations by factoring. The skills are all mixed, you will need to decide which skills are being applied and which to use.

Examples:
a. Factor out GCF Only $\mathbf{1 2 x} \mathbf{x}^{\mathbf{y}} \mathbf{y}^{2}-\mathbf{2 4} \mathbf{x}^{2} \mathbf{y}^{\mathbf{3}}+\mathbf{1 6 x} \mathbf{y}^{\mathbf{3}}$

$$
3 \cdot 4 \cdot x \cdot x \cdot x \cdot y \cdot y \cdot-6 \cdot 4 \cdot x \cdot x \cdot y \cdot y \cdot y+4 \cdot 4 \cdot x=y \cdot y \cdot y
$$

Factored: $4 x y^{2}\left(3 x^{2}-6 x y+4 y\right)$
c. Solve using Quadratic Formula: $-8 z^{2}+2 z+16=9$

$$
\begin{aligned}
& -8 z^{2}+2 z+7=0 \quad a=-8, b=2, c=7 \\
z= & \frac{-(2) \pm \sqrt{(2)^{2}-4(-8)(7)}}{2(-8)}=\frac{-2 \pm \sqrt{228}}{-16} \\
z= & \frac{-2+15.099}{-16} \text { and } z=\frac{-2-15.099}{-16} \\
z= & -0.819 \text { and } z=1.069
\end{aligned}
$$

b. Factor out GCF and Solve: $5 x^{3}-45 x=0$
$5 x\left(x^{2}+0 x-9\right)=0 \quad[3(-3)=-9$ and $3+-3=0]$
Factored: $5 x(x+3)(x-3)$

$$
5 x=0 \quad x+3=0 \quad x-3=0
$$

Solved: $x=0 \quad x=-3 \quad x=3$
d. Factor and Solve: $-p^{2}-10 p-16=0$

$$
-1\left(p^{2}+10 p+16\right)=0
$$

Factored: $-1(p+2)(p+8)=0 \quad[2(8)=16$ and $2+8=10]$

$$
p+2=0 \quad p+8=0
$$

Solved: $p=-2 \quad p=-8$

1. Factor out GCF Only: $10 x^{2} y z-22 x^{3} y^{2} z$

$$
2 x^{2} y z(5-11 x y)
$$

2. Factor Only: $-x^{2}+5 x+24$

$$
\begin{aligned}
& \text { only: }-x^{2}+5 x+24 \\
& -1\left(x^{2}-5 x-24\right) \\
& -1(x-8)(x+3)
\end{aligned}
$$

4. Factor and Solve: $m^{2}+12 m-28=0$
5. Factor out GCF and Solve: $12 b^{2}-8 b=0$

$$
\begin{aligned}
4 b(3 b-2) & =0 \\
4 b & =0 \quad 3 b-2
\end{aligned}
$$

$$
\text { and Solve: } m^{2}+12 m-28=0=0
$$

$$
\begin{array}{cc}
m+14=0 & m-2=0 \\
-14=14 & +2
\end{array}
$$

$$
\begin{array}{ll}
n+14=0 \\
-14-14 & +2+2
\end{array}
$$

$$
m=-14 \quad m=2
$$

5. Use Quadratic Formula to solve: $5 t^{2}+17 t-12=0$

$$
\begin{array}{ll}
a=5 & x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} \\
b=17 & x=\frac{-17 \pm \sqrt{(17)^{2}-4(5)(-12)}}{2(5)} \\
c=12 & x=\frac{-17+23}{10} \quad x=\frac{-17-23}{10} \\
& x=\frac{-17 \pm \sqrt{529}}{10} \quad \frac{x=0.6 \quad x=-4}{}
\end{array}
$$

6. Solve for $x$ using Square root: $64 x^{2}-1=0$ $+1$

$$
\begin{aligned}
& \frac{64 x^{2}}{64}=\frac{1}{64} \\
& \sqrt{x^{2}}=\sqrt{\frac{1}{64}} \\
& x=\frac{1}{8} \quad x=-\frac{1}{8}
\end{aligned}
$$

Set equal to 0 and then Factor or Use Quadratic Formula to solve:
7. $y^{2}+4 y=45$
$-45-45$

$$
y^{2}+4 y-45=0
$$

$$
\begin{array}{ll}
y+9=0 & y-5=0 \\
-9-9 & y+5+5
\end{array}
$$

$$
-9-9+5+5
$$

$$
(y+9)(y-5)=0 \quad y=-9 \quad y=5
$$

$$
y=-9 \quad y=5 \quad b=+3
$$

$$
\text { 9. } 18 x=2 x^{2}-72
$$

$$
0=2 x^{2}-18 x-72
$$

$$
q=2
$$

$$
\begin{aligned}
& c=12 \\
& 10 . \\
& \text { 8. } \quad 3 p^{2}=13 p-12 \\
& 3 p^{2}-13 p+12=0 \\
& \begin{array}{l}
a=3 \\
b=-13
\end{array} \quad x=\frac{-(-13) \pm \sqrt{(-13)^{2}-4(3)(12)}}{2(3)} \\
& x=\frac{3+5}{6} \quad x=\frac{3-5}{6} \\
& x=1 . \overline{3} \quad x=-.3 \\
& x^{2}-x+20=0 \\
& (x-5)(x+4)=0 \\
& \begin{array}{ll}
x-5=0 & x+4=0 \\
+5+5 & -4
\end{array} \\
& x=5 \quad x=-4
\end{aligned}
$$

