

9.1

Exponents and Radicals

Your Name

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Notes

Properties
of
Exponents

$$\begin{aligned} y^{-3} &= \frac{1}{y^3} \\ \left(\frac{2}{3}\right)^{-1} &= \frac{3}{2} \\ &= 0.6 \end{aligned}$$

$\sqrt[2]{ }$ square root
 $\sqrt[3]{ }$ cube root
 $\sqrt[4]{ }$ fourth root
 $\sqrt[5]{ }$ fifth root

$$x^2 = x \cdot x \quad \text{definition of exponent}$$

$$x^{-2} = \frac{1}{x^2} = \frac{1}{x \cdot x} \quad \text{negative exponent} = \text{flipped}$$

$$x^2 \cdot x^5 = x^{2+5} = x^7 \quad \begin{array}{l} \text{Add Exponents} \\ \text{when multiplying same bases} \end{array}$$

$$\frac{x^2}{x^5} = x^{2-5} = x^{-3} = \frac{1}{x^3} \quad \begin{array}{l} \text{Subtract} \\ \text{Exponents} \end{array}$$

$$(x^2)^5 = x^{2 \cdot 5} = (x \cdot x \cdot x \cdot x \cdot x) (x \cdot x \cdot x \cdot x \cdot x) = x^{10} \quad \text{Multiply Exponents}$$

$$\sqrt[5]{x^2} = x^{\frac{2}{5}} \quad \text{Divide Exponents}$$

Radicals and Roots

Index, Radical, Radicand

number on shelf

$\sqrt[3]{27}$ stuff under root

$$\text{determines amount needed to be the same}$$

$$\sqrt[3]{3 \cdot 3 \cdot 3} = 3$$

Even indexed radicals must have a positive number underneath as the radicand in order to be a Real number

if no index, index is 2

$$\sqrt[4]{16}$$

$\sqrt[4]{2 \cdot 2 \cdot 2 \cdot 2}$

2

$$\sqrt{-25}$$

~~$\sqrt{-5 \cdot 5}$~~

can't have negative numbers under radical

Odd indexed radicals can have a positive or negative number underneath as the radicand and be a Real number

$$\sqrt[3]{27}$$

$$\sqrt[5]{-32}$$

$\sqrt[5]{-2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}$

Division

$$2 \overline{)16}$$

b/c $8+8$

Square root

$$\sqrt{16} = 4$$

$$\underline{4} \cdot \underline{4}$$

Simplify by prime factorization

$$\sqrt{16}$$

$$\begin{array}{c} \cancel{1} \cdot \cancel{2} \cdot \cancel{2} \cdot \cancel{2} \\ \cancel{2} \cdot \cancel{2} \\ 4 \end{array}$$

$$\sqrt{75x^6}$$

$$\begin{array}{c} \cancel{3} \cdot \cancel{5} \cdot \cancel{5} \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x \\ \cancel{5} \cdot x \cdot x \cdot x \cdot \sqrt{3} \\ \boxed{5x^3\sqrt{3}} \end{array}$$

Square root
need groups
of 2

$$\sqrt{36x^{11}}$$

$$\begin{array}{c} \cancel{1} \cdot \cancel{2} \cdot \cancel{2} \cdot \cancel{3} \cdot \cancel{x} \\ \cancel{2} \cdot \cancel{3} \cdot x \cdot x \cdot x \cdot x \cdot x \cdot x \\ 6x^5\sqrt{x} \end{array}$$

Cubic root needs
groups of 3

$$\sqrt[3]{-27x^4}$$

$$\begin{array}{c} \cancel{-3} \cdot \cancel{3} \cdot \cancel{3} \cdot x \cdot x \cdot x \\ -3x^3\sqrt{x} \end{array}$$

$$\sqrt{98}$$

$$\begin{array}{c} \sqrt{7} \cdot \cancel{2} \cdot 2 \\ 7 \cdot \sqrt{2} \end{array}$$

$$\sqrt{63x^7}$$

$$\begin{array}{c} \cancel{7} \cdot \cancel{3} \cdot \cancel{3} \cdot x \cdot x \cdot x \cdot x \cdot x \\ 3 \cdot x \cdot x \cdot x \cdot \sqrt{7} \cdot \sqrt{x} \\ \boxed{3x^3\sqrt{7x}} \end{array}$$

Simplify by perfect squares

$$1^2 = 1 \rightarrow \sqrt{1} = 1$$

$$2^2 = 4 \rightarrow \sqrt{4} = 2$$

$$3^2 = 9 \rightarrow \sqrt{9} = 3$$

$$4^2 = 16 \rightarrow \sqrt{16} = 4$$

$$5^2 = 25 \rightarrow \sqrt{25} = 5$$

$$6^2 = 36 \rightarrow \sqrt{36} = 6$$

$$7^2 = 49 \rightarrow \sqrt{49} = 7$$

$$8^2 = 64 \rightarrow \sqrt{64} = 8$$

$$9^2 = 81 \rightarrow \sqrt{81} = 9$$

$$10^2 = 100 \rightarrow \sqrt{100} = 10$$

$$11^2 = 121 \rightarrow \sqrt{121} = 11$$

$$12^2 = 144 \rightarrow \sqrt{144} = 12$$

$$\sqrt{32}$$

$$\begin{array}{c} \sqrt{16 \cdot 2} \\ \boxed{4\sqrt{2}} \end{array}$$

$$\sqrt{75x^6}$$

$$\begin{array}{c} \sqrt{25 \cdot 3 \cdot x^2 \cdot x^2 \cdot x^2} \\ \sqrt{25 \cdot \sqrt{x^2} \cdot \sqrt{x^2} \cdot \sqrt{x^2} \cdot \sqrt{3}} \\ 5 \cdot x \cdot x \cdot x \cdot \sqrt{3} \\ \boxed{5x^3\sqrt{3}} \end{array}$$

$$-\left(\sqrt{36x^{11}}\right)$$

$$\begin{array}{c} \cancel{\sqrt{-252x^4}} \\ \sqrt{4 \cdot 9 \cdot 7 \cdot -1 \cdot x^4} \\ \sqrt{4} \cdot \sqrt{9} \cdot \sqrt{-7} \cdot \sqrt{x^4} \cdot \sqrt{x^2} \end{array}$$

$$\begin{array}{c} -\left(\sqrt{36x^{11}}\right) \\ -\left(6x \cdot x \cdot x \cdot x \cdot x \cdot \sqrt{x}\right) \\ -6x^5\sqrt{x} \end{array}$$

$$\begin{array}{c} 2 \cdot 3 \cdot x \cdot x \cdot \sqrt{-7} \\ 6x^2\sqrt{-7} \end{array}$$

* Imaginary, can't take $\sqrt{-}$ of negative numbers

$$\sqrt{48}$$

$$\begin{array}{c} \sqrt{16 \cdot 3} \\ \sqrt{16} \cdot \sqrt{3} \\ \boxed{4\sqrt{3}} \end{array}$$

$$\sqrt{121w^8}$$

$$\begin{array}{c} \sqrt{121} \cdot \sqrt{w^2} \cdot \sqrt{w^2} \cdot \sqrt{w^2} \cdot \sqrt{w^2} \\ 11w \cdot w \cdot w \cdot w \\ \boxed{11w^4} \end{array}$$

Homework: pg. 485 #13-20 and 37

In Exercises 13–20, simplify the expression.
(See Example 1.)

13. $\sqrt{20}$

14. $\sqrt{32}$

15. $\sqrt{128}$

16. $-\sqrt{72}$

17. $\sqrt{125b}$

18. $\sqrt{4x^2}$

19. $-\sqrt{81m^3}$

20. $\sqrt{48n^5}$

ERROR ANALYSIS In Exercises 37 and 38, describe and correct the error in simplifying the expression.

37.



$$\begin{aligned}\sqrt{72} &= \sqrt{4 \cdot 18} \\ &= \sqrt{4} \cdot \sqrt{18} \\ &= 2\sqrt{18}\end{aligned}$$

13. $2\sqrt{5}$

14. $4\sqrt{2}$

15. $8\sqrt{2}$

16. $-6\sqrt{2}$

17. $5\sqrt{5b}$

18. $2x$

19. $-9m\sqrt{m}$

20. $4n^2\sqrt{3n}$

37. The radicand 18 has a perfect square factor of 9;
 $\sqrt{72} = \sqrt{36 \cdot 2} = 6\sqrt{2}$