

Your Name

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Factoring out
GCF

Notes

Remember....

The distributive property

$$\begin{array}{l}
 4(x + 3) \\
 \underline{4 \cdot x} + \underline{4 \cdot 3} \\
 4x + 12
 \end{array}
 \quad
 \begin{array}{l}
 \text{Put GCF} \\
 \text{in front} \rightarrow \textcircled{3x}(x + 2) \\
 \text{follow} \\
 \text{for GCF} \rightarrow \underline{3x \cdot x} + \underline{3x \cdot 2} \\
 3x^2 + 6x
 \end{array}$$

$$4y^2(x + 3y)$$

Factoring

is just undoing
the distributive property!

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Factoring a
Polynomial
GCF

Always
Two or three terms: Factor out GCF FIRST. Write the GCF on the outside of the parenthesis, and the left over factors that are added or subtracted inside the parenthesis. As if you undid the distributive property

ex. $12a^2 + 3a$ what is GCF?

$$\underline{3a} \cdot \underline{4a} + \underline{3a} \cdot \underline{1} \qquad 3a$$

completely
factored

$$\boxed{3a(4a + 1)}$$

to check (distribute)

ex. $6m + 4m^2n + 8m^3n^2$

GCF?
2m

$$\underline{2m} \cdot \underline{3} + \underline{2m} \cdot \underline{2mn} + \underline{2m} \cdot \underline{4m^2n^2}$$

$$\boxed{2m(3 + 2mn + 4m^2n^2)}$$

It is the simple things in life...

The Zero Product Property



Anything times 0 equals 0

$$a(0) = 0 \quad (0)b = 0$$

if $ab = 0$ then **either b was 0 or a was 0**

Solving
Using
GCF

lead exponent determines # of solutions

$$6a^2 + 3a = 0$$

$$3a \cdot 2a + 3a \cdot 1 = 0$$

$$3a(2a + 1) = 0$$

$$3a = 0 \quad 2a + 1 = 0$$

$$\boxed{a = 0} \quad \begin{array}{r} 2a + 1 = 0 \\ -1 \quad -1 \\ \hline 2a = -1 \\ \frac{2}{2} \quad \frac{-1}{2} \\ \hline a = -\frac{1}{2} \end{array}$$

$$45y^2 - 18y = 0$$

$$9y(5y - 2) = 0$$

$$9y = 0 \quad 5y - 2 = 0$$

$$\boxed{y = 0} \quad \begin{array}{r} 5y - 2 = 0 \\ +2 \quad +2 \\ \hline 5y = 2 \\ \frac{5}{5} \quad \frac{2}{5} \\ \hline y = \frac{2}{5} \end{array}$$

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Factor each polynomial if possible

$$3m + 36$$

$$3(m + 12)$$

$$5x^2 - 35x$$

$$5x(x - 7)$$

$$4p^2q^2 - 16pq^2 + 56pq^3$$

$$4pq^2(p - 4 + 14q)$$

$$4a^3b + 28a^2b$$

$$4a^2b(a + 7)$$

~~$3x^2 = 21x$~~
 ~~$\frac{3x^2}{x} = \frac{21x}{x}$~~
 ~~$x = 7$~~

Never divide * by a variable

* Make equation = 0

$$3x^2 = 21x$$

$$-21x \quad -21x$$

$$3x^2 - 21x = 0$$

move term over

Set each factor = 0 and solve

$$3x(x - 7) = 0$$

$$\frac{3x}{3} = \frac{0}{3} \quad x - 7 = 0$$

$$\boxed{x = 0} \quad \boxed{x = 7}$$

$$-9a^2 + 63a = 0$$

$$-9a(a - 7) = 0$$

$$\frac{-9a}{-9} = \frac{0}{-9} \quad a - 7 = 0$$

$$+7 \quad +7$$

$$\boxed{a = 0} \quad \boxed{a = 7}$$

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Assignment:

pg. 381 #25-38 all

odd

and 37 and 38

In Exercises 25–30, factor the polynomial.
(See Example 3.)

25. $5z^2 + 45z$

26. $6d^2 - 21d$

27. $3y^3 - 9y^2$

28. $20x^3 + 30x^2$

29. $5n^6 + 2n^5$

30. $12a^4 + 8a$

In Exercises 31–36, solve the equation. (See Example 4.)

31. $4p^2 - p = 0$

32. $6m^2 + 12m = 0$

33. $25c + 10c^2 = 0$

34. $18q - 2q^2 = 0$

35. $3n^2 = 9n$

36. $-28r = 4r^2$

38. **ERROR ANALYSIS** Describe and correct the error in solving the equation.

X

$$\begin{aligned} 3y^2 &= 21y \\ 3y &= 21 \\ y &= 7 \\ \text{The root is } y &= 7. \end{aligned}$$

X

$$\begin{aligned} 6x(x + 5) &= 0 \\ x + 5 &= 0 \\ x &= -5 \\ \text{The root is } x &= -5. \end{aligned}$$

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Assignment Key: pg. 381 #25-37 all

25. $5z(z + 9)$

26. $3d(2d - 7)$

27. $3y^2(y - 3)$

28. $10x^2(2x + 3)$

29. $n^5(5n + 2)$

30. $4a(3a^3 + 2)$

31. $p = 0, p = \frac{1}{4}$

32. $m = 0, m = -2$

33. $c = 0, c = -\frac{5}{2}$

34. $q = 0, q = 9$

35. $n = 0, n = 3$

36. $r = 0, r = -7$

37. also need to set $6x = 0$ and solve; $6x = 0$ or $x + 5 = 0$; $x = 0$ or $x = -5$; The roots are $x = 0$ and $x = -5$.

38. cannot divide both sides by y , because y could be 0 and division by 0 is undefined; $3y^2 - 21y = 0$; $3y(y - 7) = 0$; $3y = 0$ or $y - 7 = 0$; $y = 0$ or $y = 7$; The roots are $y = 0$ and $y = 7$.