

Your Name

Mrs. T

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Notes

Lesson 7.2

Multiplying Polynomials by Monomials

Objective: To be able to multiply a polynomial by a monomial using distribution and exponent rules.

Life Lesson/Math Skill: Once we know how to distribute a monomial to a polynomials then we multiply any size polynomial by any size polynomial using distribution. Then we can do it backwards and factor!

Recall: Distributive Property- when a number on the outside of parenthesis is multiplied to each number or variable separated by an addition/subtraction sign within the parenthesis.

$$3(x + 2) \Rightarrow 3x + 6$$

Multiply using Distribution-

When a monomial outside parenthesis is multiplied to each term inside the parenthesis.

*Remember, when variables are multiplied it will effect the exponents. **addition**

$$\begin{aligned} 2y &= y + y \\ y^2 &= y \cdot y \end{aligned}$$

$$\begin{aligned} x(5x + x^2) &= x \cdot 5x + x \cdot x^2 \\ &= 5x^2 + x^3 \end{aligned}$$

$$\begin{aligned} -3x(4x^2 - 5x + 2) &= -3x \cdot 4x^2 + -3x \cdot -5x + -3x \cdot 2 \\ &= -12x^3 + 15x^2 - 6x \end{aligned}$$

$$\begin{aligned} -2xy(2y + 4x^2) &= -2 \cdot x \cdot y \cdot 2 \cdot y + -2 \cdot x \cdot y \cdot 4 \cdot x^2 \\ &= -2 \cdot 2 \cdot x \cdot y \cdot y + -2 \cdot 4 \cdot x \cdot x \cdot y \\ &= -4xy^2 - 8x^3y \end{aligned}$$

$$\begin{aligned} 2x^2y^2(3xy + 2y + 5x) &= 2 \cdot x^2 \cdot y^2 \cdot 3 \cdot x \cdot y + 2 \cdot x^2 \cdot y^2 \cdot 2 \cdot y + 2 \cdot x^2 \cdot y^2 \cdot 5 \cdot x \\ &= 2 \cdot 3 \cdot x^3 \cdot x \cdot y^2 \cdot y + 2 \cdot 2 \cdot x^2 \cdot y^2 \cdot y + 2 \cdot 5 \cdot x^3 \cdot x \cdot y^2 \\ &= 6x^3y^3 + 4x^2y^3 + 10x^3y^2 \end{aligned}$$

Simplifying -Distributing (add exponents) and combining like terms

Ex. $x(3x - 4) - 5x$

$$\begin{aligned} x \cdot 3x - x \cdot 4 - 5x &= 3x^2 - 4x - 5x \\ &= 3x^2 - 9x \end{aligned}$$

Ex. $-x(3x - 4) - 5x$

$$\begin{aligned} -x \cdot 3x + -x \cdot -4 - 5x &= -3x^2 + 4x - 5x \\ &= -3x^2 - 1x \end{aligned}$$

Let's take turns!

Ex. $6x^2(3x^2 + 2x - 6) - 3x(2x + x^2 + 3)$

$$\begin{aligned} 18x^4 + 12x^3 - 36x^2 - 6x^2 - 3x^3 - 9x &= 18x^4 + 9x^3 - 42x^2 - 9x \end{aligned}$$

$$18x^4 + 9x^3 - 42x^2 - 9x$$

$$-a^2(4a^2 - 5a) + 2a(3a + 6)$$

$$\boxed{-4a^4 + 5a^3 + 6a^2 + 12a}$$

For Stamps!

$$3pq(5p + 2q) - (2p^2q - 8q^2p + 1p^2)$$

$$\begin{array}{r} 15p^2q + \cancel{6pq^2} - 2p^2q + \cancel{8q^2p} - 1p^2 \\ \hline 13p^2q + 14pq^2 - 1p^2 \end{array}$$

$$5y(x^3 + 2xy + y^2) + xy(4x^2 - \cancel{1}xy - 2y) - 3y^3$$

$$\begin{array}{r} 5yx^3 + \cancel{10xy^2} + 5y^3 + 4x^3y - \cancel{x^2y^2} - \cancel{2xy^2} - 3y^3 \\ \hline 9yx^3 + 8xy^2 + 2y^3 - x^2y^2 \end{array}$$

$$9yx^3 + 8xy^2 + 2y^3 - x^2y^2$$

Solving
equations

For Stamps!

$$\begin{array}{r} -2(3a - 2a^2) = 4a(5 + a) \\ -6a + \cancel{4a^2} = 20a + \cancel{4a^2} \\ \underline{-6a} \quad \underline{-4a^2} \\ -6a = 20a \\ +6a \quad +6a \\ \hline 0 = 26a \\ \frac{0}{26} = \frac{26a}{26} \\ a = 0 \end{array}$$

$$6x(x+2) = 2(3x^2 + 12)$$

$$\begin{array}{r} 6x^2 + 12x = 6x^2 + 24 \\ -6x^2 \quad -6x^2 \\ \hline 12x = 24 \\ \frac{12x}{12} = \frac{24}{12} \\ x = 2 \end{array}$$

$$2(9y + 4 - 2y) = -3(6y - 2) + 9(3 - 7y)$$

$$\begin{array}{r} 18y + 8 - 4y = -18y + \cancel{6} + \cancel{27} - \cancel{63y} \\ 14y + 8 = -18y + 33 \\ +81y \quad +81y \\ \hline 95y + 8 = 33 \\ -8 \quad -8 \\ \hline 95y = 25 \\ \frac{95y}{95} = \frac{25}{95} \\ y = \frac{5}{19} \end{array}$$

Summary

Objective: To be able to multiply a polynomial by a monomial using distribution and exponent rules.

Virtue/Skill: Once we know how to distribute a monomial to a polynomials then we multiply any size polynomial by any size polynomial using distribution. Then we can do it backwards and factor!

Assignment: Workbook 7-5

Homework Answers 7-5:

1. $4a^2 + 3a$
2. $-11c^2 - 4c$
3. $2x^2 - 5x$
4. $2y^2 - 8y$
5. $-3n^3 - 6n^2$
6. $12h^2 - 20h$
7. $15x^3 - 3x^2 + 12x$
8. $35c - 14c^3 + 7c^4$
9. $-4b + 36b^2 + 8b^3$
10. $-30y - 6y^2 + 24y^3$
11. $4m^4 + 6m^3 - 10m^2$
12. $6n^4 - 9n^3 - 12n^2$
13. $3w^2 + 7w$
14. $5f^2 - 5f$
15. $-2p^2 + 3p$
16. $-4y^3 - y^2$
17. $3x^3 + 8x$
18. $20a^3 - 7a$
19. $-22b^2 + 2b + 8$
20. $6m^2 + 6m - 3$
21. -7
22. 4
23. -5
24. -6
25. -2
26. 1