

<p>Goal 1: Do you recognize the type of model that is present? Goal 2: Can you determine the rate of change as a decimal? Goal 3: Can you determine the rate of change as a percent? Goal 4: Can you complete a table related to the population over time? Goal 5: Do you know the initial population from the model? Goal 6: Can you connect the graph of the model to its function? Goal 7: Can you label points from a table on the graph of a model? (including its initial point)</p>	<p>Model 1 $A(x) = 100(1+r)^x = 100(0.88)^x$ $A(0)$ = population at time 0 = 100 Related Point (0, 100) $A(5)$ = population at time 5 = 53.7732 Related Point (5, 53.7732) $A(10)$ = population at time 10 = 27.8501 Related Point (10, 27.8501) $A(15)$ = population at time 15 = 14.6974 Related Point (15, 14.6974)</p> <p>Population over time doesn't make sense max 100 $A = P(1+r)^t$ $n) = 100(0.88)^t$ (5, 53.8) (10, 27.9) (15, 14.7) time since initial observation Time</p>
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For model 1

What type of model is present? Decay growth or decay Base = 0.88
 What is the rate of change as a decimal? -0.12 Solve for r: $1+r = 0.88$
 What is the rate of change as a percentage? -12% $r = -0.12$

What was the initial population? 100

What does the point (15, 14.7) mean? The 15 tells us time while the 14.7 tells us population

(the unit of time was not specifically mentioned but it can be seconds, minutes, hours, decades, etc. it just depends on scenario and population we are observing)

The domain of this model is [0, 100] x values The range of population in this model is (0, 100] y values
 we technically can never reach 0 min max

“Other” Questions that you might be asked to do when given the model, like this scenario

- Complete the table related to the given model (Remember 2^{nd} Graph makes a table with TI 84) $Y = 100(0.88)^x$

X	0	1	2	3	4	5	6
A(x)	100	88	77	68	59	52	46

77.44 68.14 59.27
 Round down

- When does this population reach 1/2 of its initial population?

1. This simply asking you to:

1/2 of 100 is 50 Initial

1. know that 1/2 of the initial population is 50 = A

2. solve the equation $50 = 100(0.88)^x$

Solve for 100 1.00
 exponent $0.5 = .88^x$

$$\log_{.88}(0.5) = x$$

$$\frac{\log(0.5)}{\log(0.88)} = x$$

- When does this population fall below 75? = A

1. This simply asking you to: Interval

1. solve the equation $75 = 100(0.88)^x$

$$0.75 = 0.88^x$$

$$\log_{.88}(0.75) = x$$

$$\frac{\log(0.75)}{\log(0.88)} = x$$

2. state the INFINITELY many solutions using a set notation or inequality

$$2.25 < x$$

- When does this population exceed 16?

$$x \in (2.25, \infty)$$

1. This simply asking you to:

1. solve the equation $16 = 100(0.88)^x$

$$0.16 = 0.88^x$$

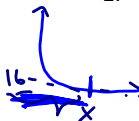
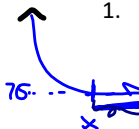
$$\log 0.16 = \log(.88)^x$$

$$\log 0.16 = x \cdot \log(.88)$$

2. state the INFINITELY many solutions using a set notation or inequality

$$0 < x < 14.336$$

$$x \in [0, 14.336) \quad \frac{\log 0.16}{\log 0.88} = x$$



$$1 + \underbrace{r}_{0.25} = 1 + r$$

Practice for you

- Given model $A(x) = 200(1.25)^x$

What type of model is present? growth or decay

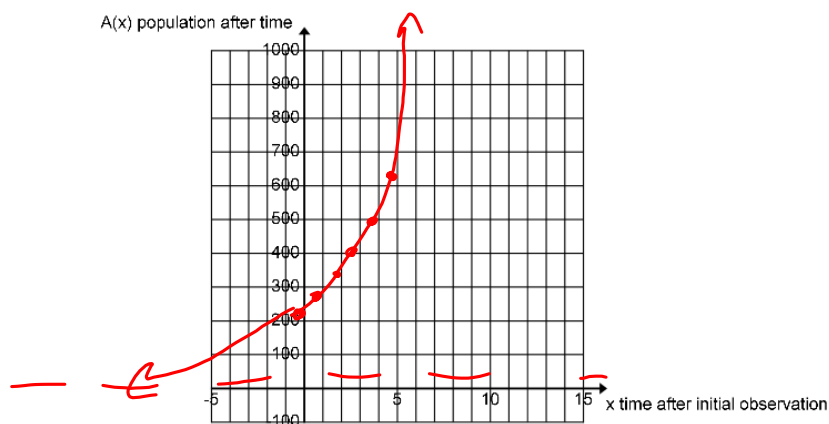
What is the rate of change as a decimal? 0.25 What is the rate of change as a percentage? 25%

What was the initial population? 200

Complete the table related to the given model (Remember 2nd Graph makes a table with TI 84 or just plug in these x values into the function on any calculator)

X	0	1	2	3	4	5	6
A(x)	200	250	312.5	390.63	488.28	610.35	767.94

Sketch a graph of A(x) label at least three points ONE POINT MUST be the y intercept



- When does this population reach DOUBLE its initial population?
 $t = ?$

$$\frac{5200}{200} = \frac{200(1.25)^t}{200}$$
- When does this population fall below 400?
 $t \in (0, 3.106)$
 $2 = 1.25^t$ Method 2
- When does this population exceed 525?
 $t \in (3.664, \infty)$
 $\log_{1.25}(2) = \log_{1.25}(1.25^t)$
 $\frac{\log(2)}{\log(1.25)} = t$
 $t = 3.106$

$$\frac{525}{200} = \frac{200(1.25)^t}{200}$$

$$2.625 = 1.25^t$$

exponents
base

$$\log_{\boxed{1.25}}(\boxed{2.625}) = \boxed{t}$$

base → exponents

$$\frac{\log(2.625)}{\log(1.25)} = t = 3.664$$

Practice for you

$1+r = 4$
 $r = 3$ positive

5. Given model $A(x) = 50(4)^x$

What type of model is present? growth or decay

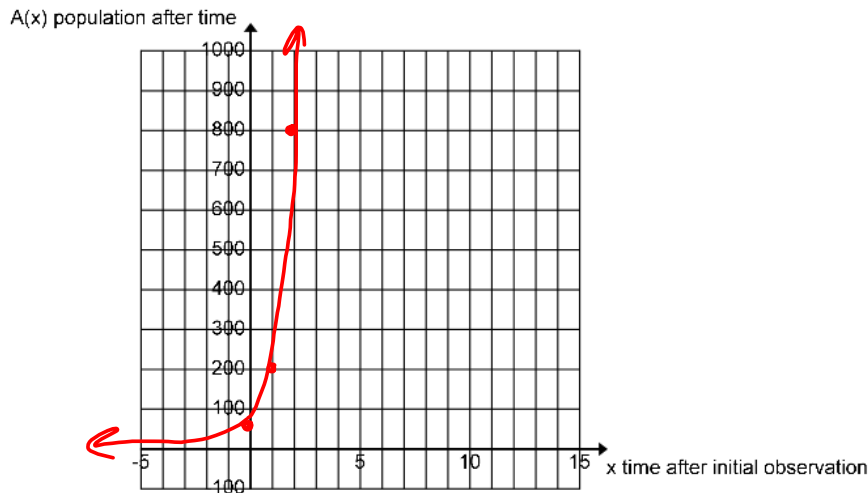
What is the rate of change as a decimal? 3 What is the rate of change as a percentage? 300%

What was the initial population? 50

Complete the table related to the given model (Remember 2nd Graph makes a table with TI 84 or just plug in these x values into the function on any calculator)

X	0	1	2	3	4	5	6
A(x)	50	200	800	3200	12800	51200	204800

Sketch a graph of A(x) label at least three points ONE POINT MUST be the y intercept



6. When does this population reach TRIPLE its initial population?

$50 \cdot 3$

$\frac{150}{50} = \frac{50(4)^x}{50}$

$3 = 4^x$
 $\log_4(3) = x$
 $x = 0.792$

7. When does this population fall below 150?

$x \in [0, 0.792)$

8. When does this population exceed 25?

The entire time it starts bigger than 25 at 50 and grows.

$25 = 50(4)^x$
 $0.5 = 4^x$
 $\log_4(0.5) = x$
 $x = -0.5$