

Your Name

Mrs. T

11/18/2020

Notes

3.5

Slope- Intercept Form and Graphs

Objective: To be able to write an equation of the line given the slope and y-intercept, written or from a graph. To be able to graph an equation using the slope and intercept.

Life Lesson/Skill: Many things are a sum of their parts, and equations for lines are no different.

Before we graph other functions that have y-intercepts, we need to be able to graph linear equations. We will be graphing multiple lines on a plane, so the graphing part needs to be easy.

slope-
intercept
form

$$y = mx + b$$

m is the slope (steapness/incline,
the amount that's added every time)

b is the y-intercept (where it starts
on y axis)

Determine the
Slope and
y-Intercept

Given: Slope
Intercept Form

Slope is # in front of x

y-intercept is # added and is (0, b)

$$\text{ex. } y = -3x - 5$$

$$\text{slope: } m = -3 = \frac{-3}{1} = \frac{3}{-1}$$

$$\text{Y-intercept: } (0, -5)$$

$$b = -5$$

$$y = \frac{2}{3}x + 9$$

$$\text{slope: } m = \frac{2}{3} = \frac{-2}{-3} = 0.\bar{6}$$

$$\text{Y-intercept: } (0, 9)$$

$$b = 9$$

Examples: Write the slope and y -intercept of each line.

1) $y = \frac{2}{3}x - 5$ 2) $y = -\frac{3}{5}x - 3$

$b = -5$ $(0, -5)$ $b = -3$ $(0, -3)$

$m = \frac{2}{3} = \frac{-2}{-3} = 0.\bar{6}$ $m = -\frac{3}{5} = \frac{-3}{5} = \frac{3}{-5} = -0.6$

3) $y = 4x + 3$ 4) $y = \frac{7}{6}x - 8$

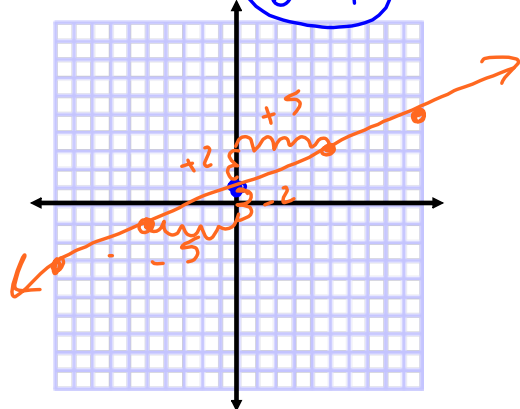
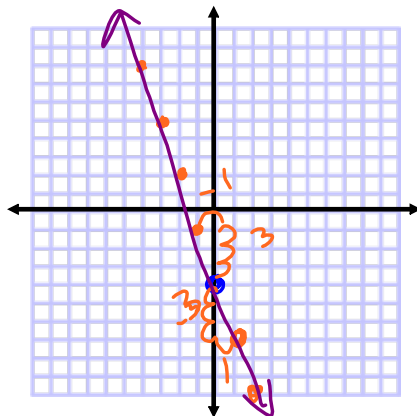
$b = 3$ $(0, 3)$ $b = -8$ $(0, -8)$

$m = 4 = \frac{4}{1} = \frac{-4}{-1}$ $m = \frac{7}{6} = \frac{-7}{-6} = 1.\bar{1}$

Graphing a Line

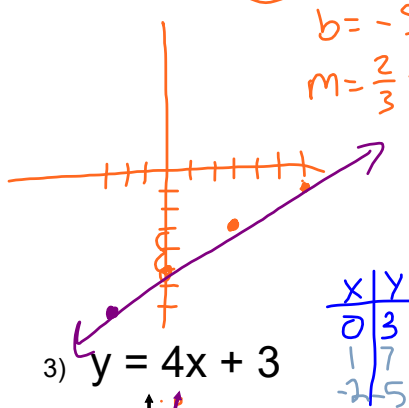
1. Make a point at the y-intercept $(0, b)$
2. From the point move up and over the slope and make a point where you finish
3. Connect the points with a straight line

$(0, b)$
 $(0, -4)$ $m = -3 = \frac{-3}{1} = \frac{3}{-1}$ $y = \frac{2}{5}x + 1 = 0.2$
 $b = 1$

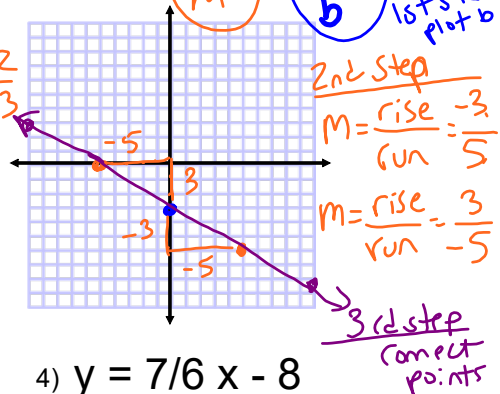


Graph each equation using slope and y intercept.

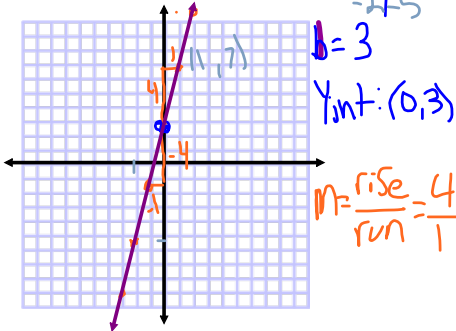
1) $y = \frac{2}{3}x - 5$



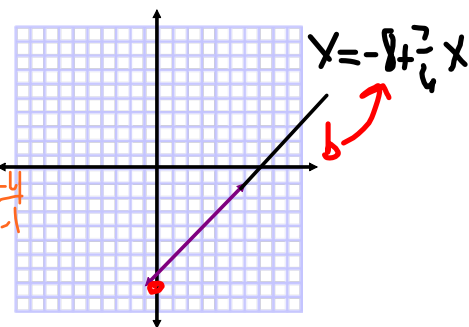
2) $y = -\frac{3}{5}x - 3$



3) $y = 4x + 3$

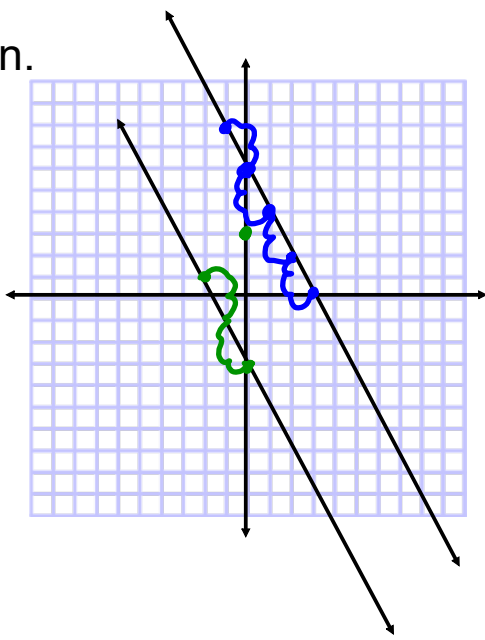


4) $y = \frac{7}{6}x - 8$



Graph the equation.

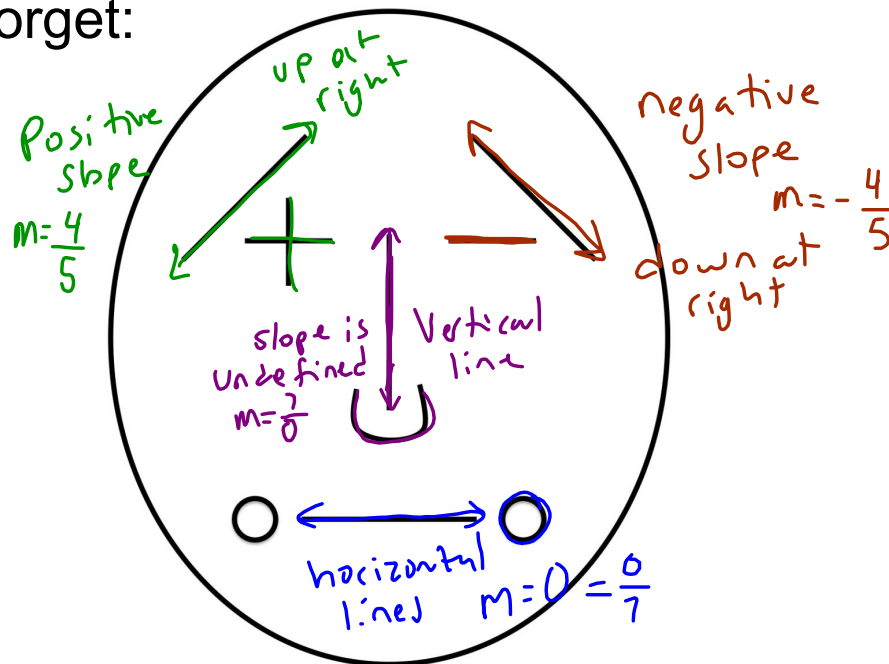
- ① $y = -2x + 6$
 ② $m = -\frac{2}{1}$ $b = 6$
 ③ (0, 6) down 2 right 1



- $4x + 2y = -6$
 $-4x \quad -4x$
 $\frac{2y}{2} = \frac{-4x + 6}{2}$
 ① $y = -2x + 3$
 ② $m = -2 = -\frac{2}{1}$ $b = 3$
 ③ plot (0, 3)
 ③ move $-\frac{2}{1}$

Quiz Review

Don't forget:



MR. SLOPE GUY

Finding Slope from Points

1. label the first coordinates x_1 and y_1
2. label the second coordinates x_2 and y_2
3. Substitute and simplify

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\begin{array}{cc} \text{1st} & \text{2nd} \\ (13, -5), & (-9, 6) \\ x_1, y_1 & x_2, y_2 \end{array}$$

$$(5, -4), (7, -4)$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$(2, -3), (2, 8)$$

$$(-1, -3), (-2, -8)$$

-

Examples: Write the slope and y-intercept of each line.

$$1) y = \underline{\frac{2}{3}}x - \underline{5}$$

$$2) y = -\frac{3}{5}x - 3$$

$$b = \quad (0, \underline{\quad})$$

$$m = \quad = \quad =$$

$$3) y = 4x + 3$$

$$4) y = \frac{7}{6}x - 8$$

Graph the following linear equation using **slope** and **y-intercept**.

$$y = \frac{2}{3}x - 1$$

Steps

1) Find the **slope** and **y-intercept**.

$$m = \frac{2}{3}$$

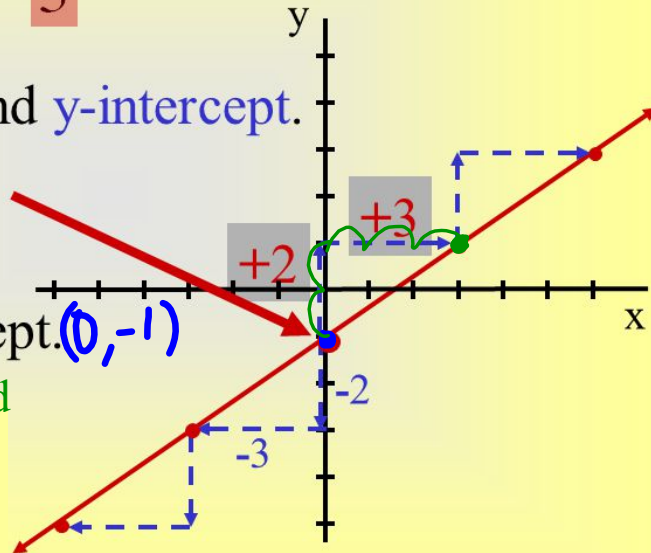
$$b = -1$$

2) Plot the y-intercept. $(0, -1)$

3) Move the slope, and plot 2nd point

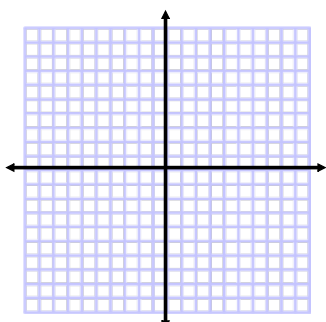
$$m = \frac{2}{3} \text{ or } m = \frac{-2}{-3}$$

4) Draw line through points.

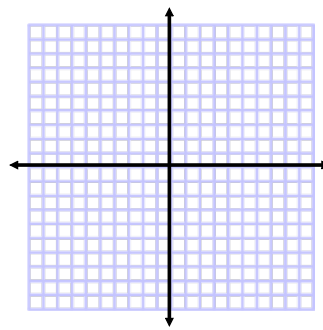


Graph each equation using slope and y intercept.

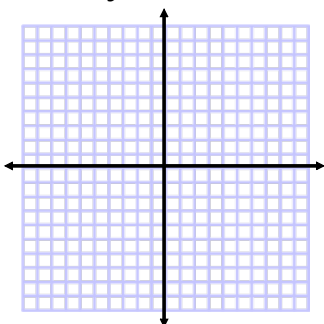
1) $y = \frac{3}{4}x - 3$ $m = \frac{\text{rise}}{\text{run}}$ $-3 = b$



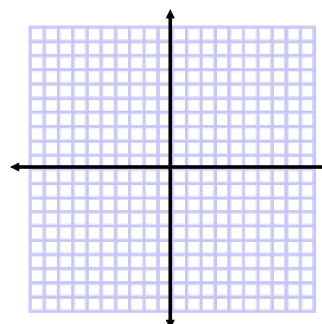
2) $y = -x + 2$



3) $y = -5/6x$

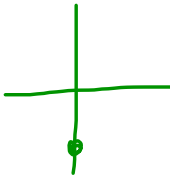


4) $y = x - 8$



Writing a Slope Intercept Equation for a Line

Given: Slope and y-intercept



Think! What do I need to write a linear equation?

1. plug y-intercept in for b
2. plug the slope in for m in to

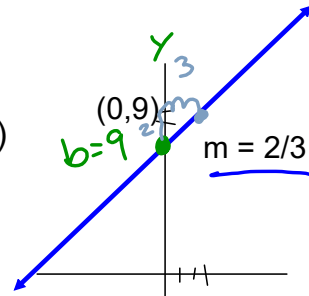
$$y = mx + b$$

ex. 1) $(0, -5), m = -3$

x is 0
 -5 is b

$$y = -3x + -5$$

ex. 2)



$$y = \frac{2}{3}x + 9$$

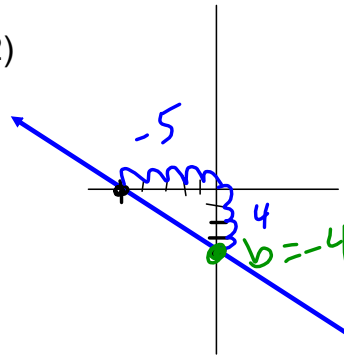
$m = \frac{2}{3}$
 $b = 9$

Examples: Write the equation for the Line

1) $(0, 7), m = \frac{2}{3}$

$$y = \frac{2}{3}x + 7$$

2)



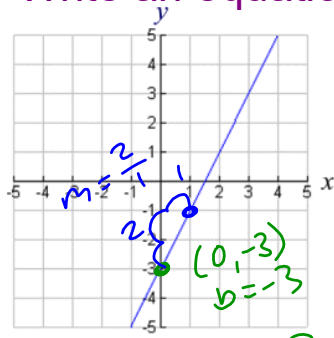
$$y = -\frac{4}{5}x + -4$$

3) $(0, 3), m = 4$

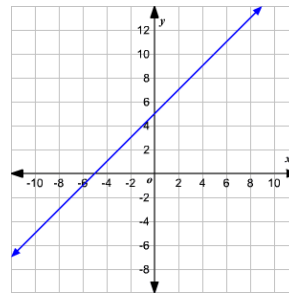
$$y = \underline{\hspace{1cm}}x + \underline{\hspace{1cm}}$$

4) $(0, -8), m = \frac{7}{6}$

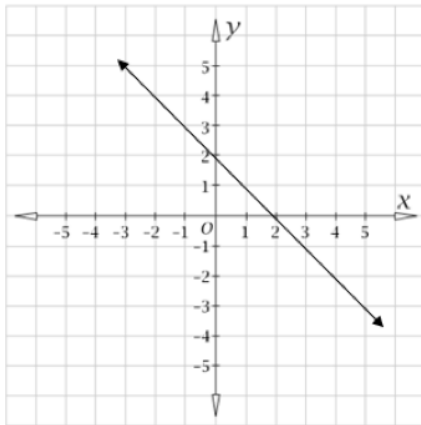
Write an equation in slope intercept form.



$$y = 2x + -3$$



$$y =$$



$$y =$$

$$(0, 3) \quad (7, 8)$$

$$m = \frac{y_1 - y_2}{x_1 - x_2} = \frac{3 - 8}{0 - 7} = \frac{-5}{-7} = \frac{5}{7}$$

$$m = \frac{5}{7}$$

Examples: Write the equation for the Line

1) x is 0 so $y = b$
 $(0, -5)$ $m = 2/3$

$$y = \frac{2}{3}x + -5$$

m slope
b y intercept
 $b = -5$

$$y = \frac{2}{3}x - 5$$

2) $(0, 0)$
 $(0, -3)$
 $m = \frac{3}{-5}$
 $b = -3$

$$y = -\frac{3}{5}x + -3$$

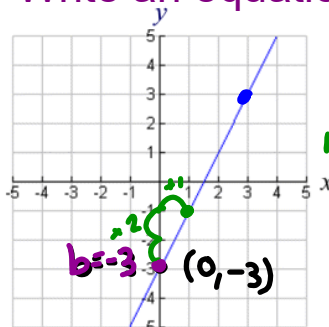
3) $(0, 3)$ $m = 4$
 $b = 3$

$$y = 4x + 3$$

4) $(0, -8)$ $m = \frac{7}{6}$
 $b = -8$

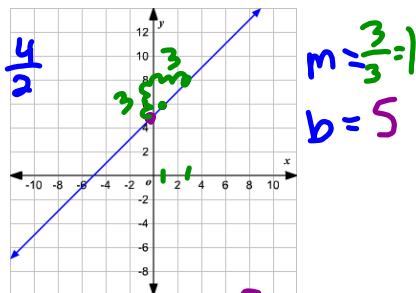
$$y = \frac{7}{6}x + -8$$

Write an equation in slope intercept form.



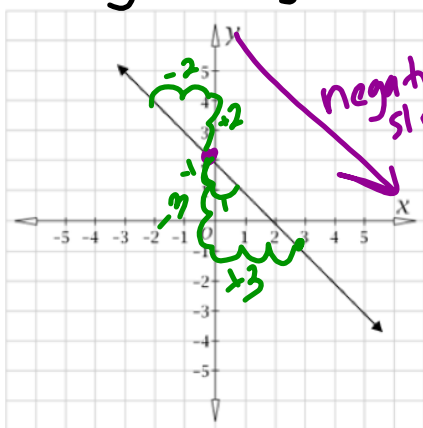
$$y = 2x + -3$$

$$y = 2x - 3$$



$$y = 1x + 5$$

$$y = x + 5$$



$$y = -x + 2$$

Write a linear equation in slope intercept form to model the situation.

The car mechanic charges \$75 for the consultation and \$45 per hour.

$x = \# \text{ hrs}$
worked
 $y = \text{total earned}$

$$m = 45$$

amount
affected
by change
1 per
'for each'

$$b = 75$$

starting amount

$(0, 75)$

$(0 \text{ hrs}, \$75)$

$$y = 45x + 75$$