

Your Name

Mrs. T

10 / 8 / 2020

Notes

# 2.3

## Solving Inequalities by Multiplication and Division

Objective: To be able to solve inequalities using multiplying and dividing. To be able to graph inequality solutions found. To understand what the solutions are.

Virtue/Skill: When we graph inequalities we might need to solve for a variable in order to graph it. With two variables on a coordinate plane, we need to be able to check our solutions to understand how to shade. Graphing on a number line is similar to graphing on a coordinate plane.

Solving Multiplication/Division Inequalities

To solve: pretend like it is an = sign and do what you have always done

**One Catch...**

*if you have to multiply or divide by a negative number on both sides to isolate the variable...you must flip the inequality sign.*

**FLIP**  
 $-5 \cdot \left(\frac{x}{5}\right) > (-2) \cdot (-5)$   
 $x < 10$   
 -5 is a negative number

**DON'T FLIP**  
 $9x < -81$   
 $\frac{9x}{9} < \frac{-81}{9}$   
 $x < -9$   
 not a negative number

Number line for  $x < 10$ : points at 9, 10, 11. Arrow points left from 10. Labels: "smaller" and "bigger".

$3 \cdot 4 = 3 \text{ groups of } 4$   
 $4 + 4 + 4$

$3x = x + x + x$   
 $3 \cdot x$

Solve and Graph

Yes Flip	No flip	Flip	No Flip
$-3y < 15$	$7m \leq 21$	$-z < 3$	$5(t \geq 2) \cdot 5$
$\frac{-3y}{-3} < \frac{15}{-3}$	$\frac{7m}{7} \leq \frac{21}{7}$	$\frac{-z}{-1} < \frac{3}{-1}$	$5 \cdot (t \geq 2) \cdot 5$
$y > -5$	$m \leq 3$	$z > -3$	$t \geq 10$

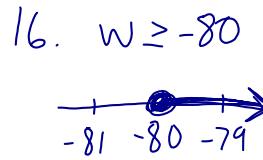
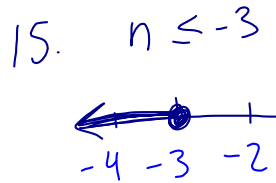
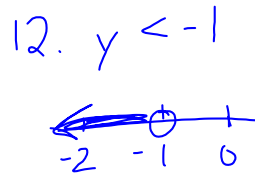
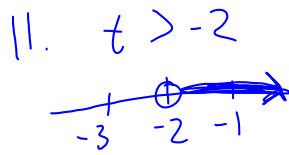
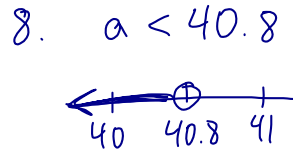
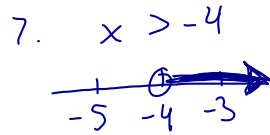
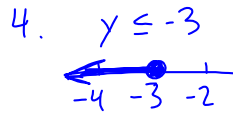
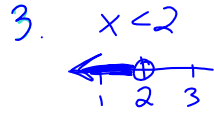
Number lines for  $y > -5$ ,  $m \leq 3$ ,  $z > -3$ , and  $t \geq 10$ .  
 -  $y > -5$ : number line from -6 to -4, arrow points right from -5. Labels: "smaller", "bigger".  
 -  $m \leq 3$ : number line from 2 to 4, arrow points left from 3.  
 -  $z > -3$ : number line from -6 to 0, arrow points right from -3.  
 -  $t \geq 10$ : number line from 9 to 11, arrow points right from 10.

What if we didn't flip the sign?

$y < -5$   
 Check  $-6$   
 $-3y < 15$   
 $-3(-6) < 15$   
 $18 < 15$   
 not true

Homework Key: Textbook pg. 71

# 3,4,7,8,11,12,15,16



If the variable is on the right

Rewrite it (before you start or at the end) keeping the expression on the bigger end still on the bigger end.

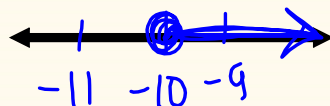
*Rewrite before you begin*

$$40 \geq -4x$$

$$\frac{-4x \leq 40}{-4} \quad \frac{40}{-4}$$

*Flip sign b/c you divided by a negative number!*

$$x \geq -10$$

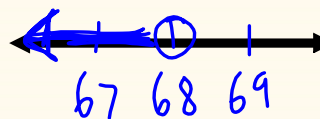


$$(-2)(-34) < \left(\frac{p}{-2}\right)(-2)$$

*Flip sign b/c you multiplied by a negative number*

$$68 > p$$

$$p < 68$$



*Rewrite so variable is on left at the end*

How do we divide fractions?

$$\frac{5}{6} \div \frac{2}{3}$$

skip Flip  
 $\frac{5}{6} \cdot \frac{3}{2}$   
 & multiply

Solving  
Inequalities  
with  
Fractions

To "divide" by the fraction, multiply  
by the reciprocal (multiply by the  
flipped fraction)

$$\left(\frac{+3}{2}\right)\left(\frac{+2x}{3}\right) > (9)\left(-\frac{3}{2}\right)\left(\frac{2x}{1}\right) - 36 < \left(\frac{1p}{2}\right)\frac{2}{1}$$

Flip  
sign b/c

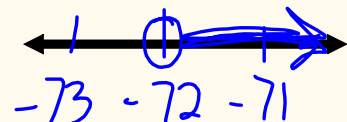
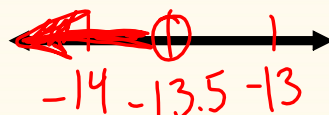
$$x < \frac{-27}{2}$$

$$x < -13.5$$

$$-72 < p$$

$$p > -72$$

No flip  
b/c  
rewrite



Write  
Multiplication  
and Division  
Inequalities

A number  $x$  divided by fifteen is greater than or equal to sixty.

$$\frac{x}{15} \geq 60$$

A number  $x$  multiplied by negative two thirds is less than zero.

$$-\frac{2}{3}x < 0$$