

Your Name

Mrs. Theo

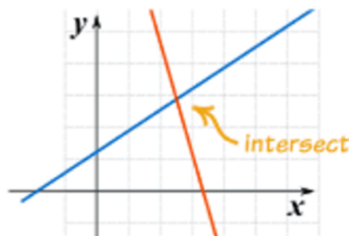
10/28/2020

Notes

Lesson 1.4 - Solving Systems of 3 Variable Equations

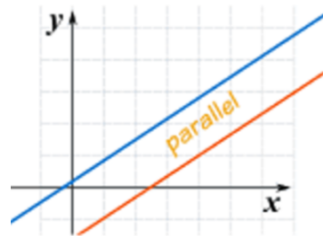
No Solution/Infinitely Many Solutions

Systems of 2 Linear Equations

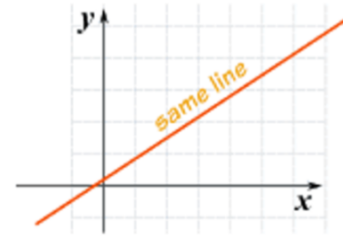


One Solution

Solve and end up with a solution (x,y) .



No Solution



∞ Solutions

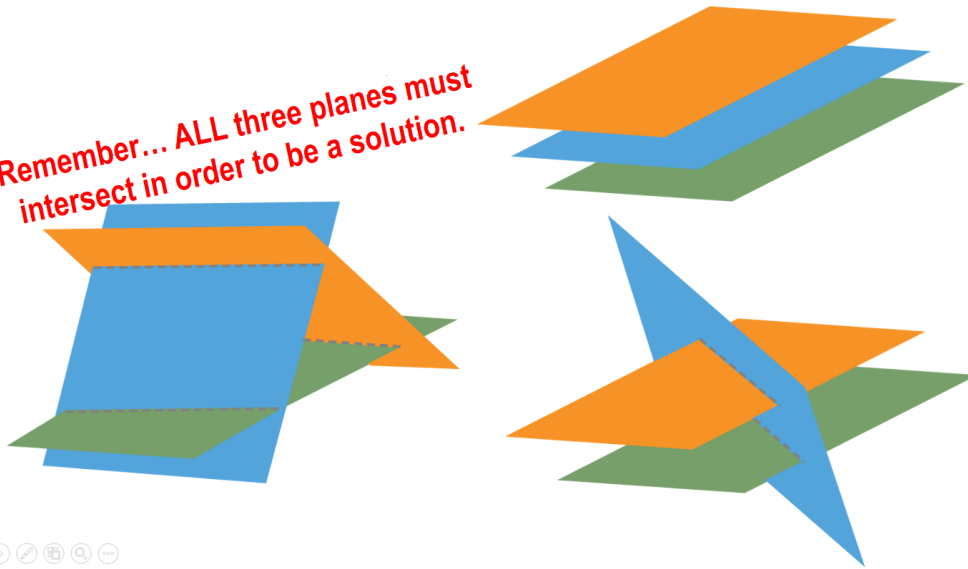
When solving, both variables are eliminated! Look at the statement that is left when the variables are gone.

False = No Solution
 $0 = 5$ or $1 = 10$

True = Infinite Solutions
 $0 = 0$ or $5 = 5$

What if there is NO solution?

Remember... ALL three planes must intersect in order to be a solution.



Systems with No Solution

If you eliminate a variable and all three variables cancel and you get a false statement

Three Variable Equations with NO solutions...

$$\begin{aligned} -3(x+y+z) &= -6 && \text{Equation ① multiply by } -3 \\ 3x+3y+3z &= 14 && \text{Equation ②} \\ x-2y+z &= 4 && \text{Equation ③} \end{aligned}$$

Two is company
Three is a crowd
Pick a variable &
KICK IT OUT!

$$\begin{aligned} \text{①} \quad & -3x-3y-3z = -6 \\ \text{②} \quad & 3x+3y+3z = 14 \end{aligned}$$



Since this is a false equation, you can conclude the original system of equations has no solution.

$$0=8$$

And... you're done!
There isn't a solution to find.

What is the graphical situation here?

2 parallel planes and one intersecting plane

Parallel Planes if: $ax + by + cz$ can be the same but with different d

Same Planes if: $ax + by + cz$ and d can be exactly the same

Ex2: Solve the system.

$$\begin{cases} x + y + z = 1 \\ 6x + 9y - 12z = 14 \\ 12x + 18y - 24z = -11 \end{cases}$$

Be smart
Check for any parallel planes

2:2
2:2

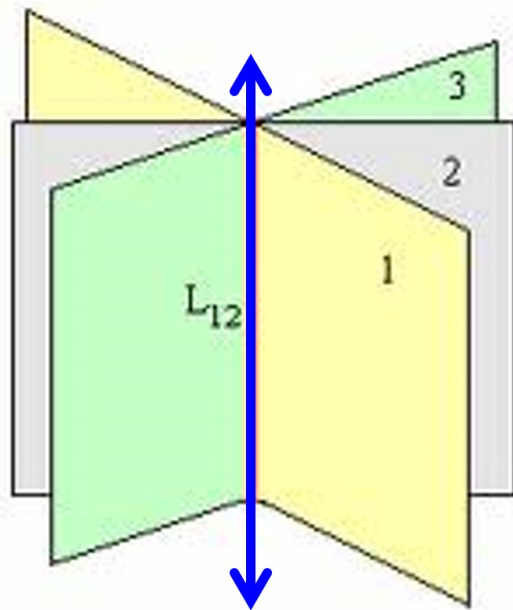
2 and 3 Parallel

No Solution

Two is company
Three is a crowd
Pick a variable &
KICK IT OUT!

KEEP CALM
THERE MAY BE
NO SOLUTION

What if there are **INFINITE** solutions?
How do I find the intersection points if the planes intersect in a **LINE**?



Systems with Infinite Solutions

1. If as you eliminate a variable, and two variables cancel and you are immediately left with one variable = a number

OR you eventually get a true statement like $0 = 0$

What happens when three planes intersect in a LINE?

Solve the system.

$2x + y + z = 0$ Equation 1

$x - 2y - 2z = 0$ Equation 2

$x + y + z = 0$ Equation 3

SOLUTION

$-2y - 2z = 0$ Equation 2
 $-x - y - z = 0$ -1 times Equation 3
 $-3y - 3z = 0$ New Equation 2
 $2x + y + z = 0$ Equation 1
 $-2x - 2y - 2z = 0$ -2 times Equation 3
 $-y - z = 0$ New Equation 1
 $-3y - 3z = 0$
 $3y + 3z = 0$
 $0 = 0$

You are NOT DONE!

Identify... many solutions

2. Take the common equation and solve for one variable, this is the expression for that coordinate in the triple.

$-y - z = 0$ Step 2
 Solve for y
 $y = -z$

3. Then substitute the two expressions for the two variables in to an original equation to get the expression for the other variable.

So the y coordinate is $-z$, the equation is in terms of z so the z coordinate will be itself

$(0, -z, z)$

(x, y, z)
 step 3
 $x + y + z = 0$
 $x + (-z) + z = 0$
 $x = 0$



Solve the system using any algebraic method.

Two is company, Three is a crowd Pick a variable & KICK IT OUT!

$(1) x + 2y - z = 4$ (4)
 $(2) 3x - y + 4z = -2$
 $(3) 6x + 5y + z = 10$

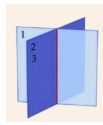
$(1) x + 2y - z = 4$
 $(3) 6x + 5y + z = 10$
 $7x + 7y = 14$
 $(1) 4x + 8y - 4z = 16$
 $(2) 3x - y + 4z = -2$
 $-1(7x + 7y = 14)$

$7x + 7y = 14$
 $+ 7x + 7y = 14$
 $-7x + 7y = 14$
 $0 = 0$ I.M.S.

$7x + 7y = 14$
 $7x = -7y + 14$
 $x = -y + 2$
 x, y
 $(-y + 2, y, y - z)$

since equation is in terms of y y is itself

$x + 2y - z = 4$
 $(-y + 2) + 2y - z = 4$
 $y + 2 - z = 4$
 $-y - z = 2$
 $2 - z = -y + 4$
 $-2 - z = -y + 2$
 $-z = -y + 2$
 $z = y - 2$



① $2x + 2y + 2z = -2$

② $(2x + 3y + 2z = 4)(-1)$

③ $(x + y + z = -1)(-2)$

① $2x + 2y + 2z = -2$

② $-2x - 3y - 2z = -4$

$-y = -6$

$y = 6$

① $2x + 2y + 2z = -2$

③ $-2x - 2y - 2z = 2$

①+③ $0 = 0$
are the same plane

going to be a line of solutions because exactly 2 variables canceled

To find x and y you can plug in $y=6$ into any of the three

See! they both give you the same equations!
③ $x + y + z = -1 \rightarrow x + 6 + z = -1$
and $x + z = -7$

② $2x + 3y + 2z = 4 \rightarrow 2x + 3(6) + 2z = 4$

$2x + 2z = -14$

$x = -z - 7$

original equations to get the new equation that you solve for one variable for and the other is itself

$(-z - 7, 6, z)$